

Three detectors gives six measured quantities (x,y in each).

- Four of these give measurements we want:

(x,y) of centre of circle

radius of circle

starting point on circle (relative size of px and py)

- Two more can be used for constraints

To be conservative, I say that the radius of the circle in the third detector is used as a cross check and the position around the circle can be used to throw out wrong combinations. (This complication was motivated by somehow thinking that background from straight tracks is more nasty than curly ones).

Now, the probability that three random points satisfy this criterion is:

$P3 = md/c = 4 \ge 0.5 / 500$ $= 0.4\%$	c = circumference of circle m = 'roadwidth' for finding track in units of pixels/fibres
	d = size of each pixel

If we add another detector, we get two more constraints we can use to eliminate fake combinations of points. Generalising to N detectors,

PN =
$$(md/c)^{N-2} (md \ 2\pi/c)^{N-3}$$

Now calculate some numbers. Let

a = #hits in *EACH* detector within time window

	N=3	N=4	N=5
PN	4 e -3	4 e -7	1 e -10
a= 2	0.032	6 e –6	1 e -9
a = 10	4	4 e -3	4 e -7
a = 100	4000	40	0.4

(This is with c = 500mm (r = 15cm), d = 0.5mm, m = 4)

Figure 2: slide 2

That was all where 'hit' meant spacepoints. OK for pixels, but for fibres (or other projective detector), we have to combine hits on each fibre to make spacepoints.

[*Discussion ommitted*]

f = fraction of detector area within 'roadwidth'

3 planes, no inefficiencies	$p_3 = f a^3 + a (1-f)$
3 planes, one inefficiency	$q_{3} = 3 a^{2} - 2 a$
4 planes, no inefficiencies	$p_4^3 = f^2 a^4 + a (1-f^2)$
4 planes, one inefficient plan	ne $q_4 = 4 f a^3 + a (1-4f)$

... Slightly more sophistication...

... Plots combining these probabilities to make spacepoints from hits with the probabilities to make tracks from spacepoints (as on previous slide).

Conclusions

- * Calculations of combinations of spacepoints to tracks and (for fibres) hits to spacepoints.
- * No matter what happens, we are dead very quickly as the rate goes up.
- * We are discussing the difference of whether a=3 is the limit or a=5, but not a=10. Therefore, we cannot beat a high rate with the detectors – the rate must not be there in the first place.
- * a depends on the time window and the road width these should be made small if we fear a high rate.

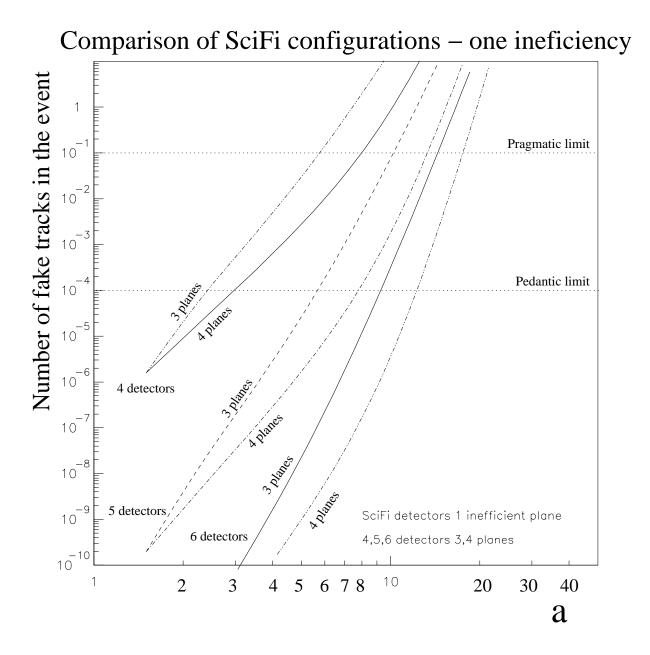


Figure 4:

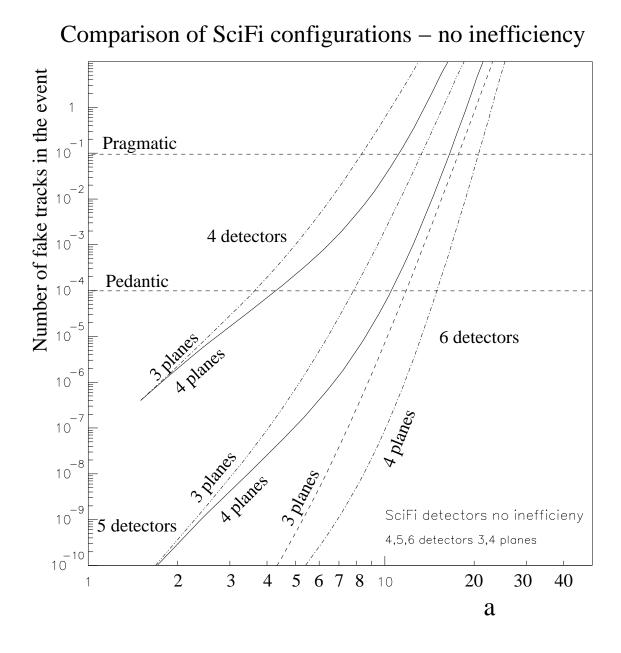
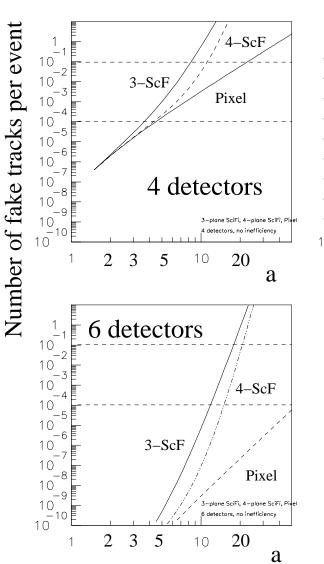
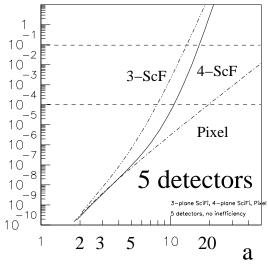


Figure 5:



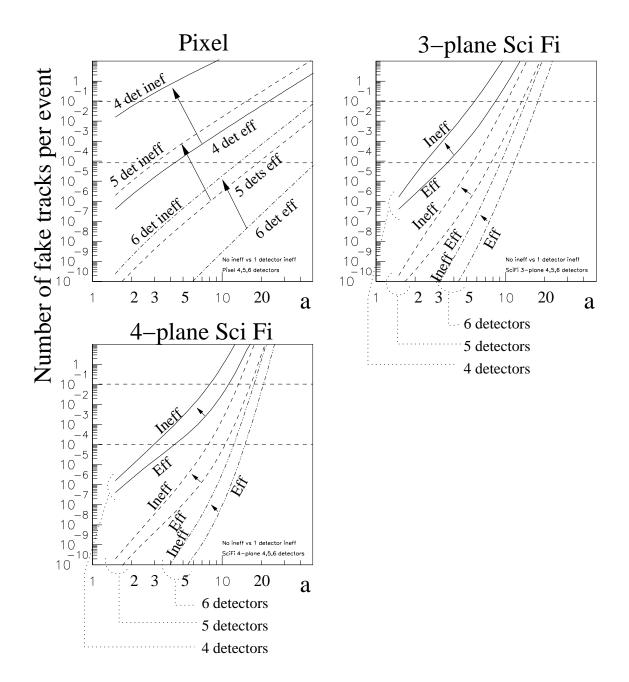
Compare detector types with same number of detectors of each type.



Note: a depends on the time window obtainable with each detector type. a = (rate) x (time window)

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Figure 6:



Compare effect of allowing an inefficient Sci–Fi plane or an inefficient Pixel detector

Figure 7: